

Theorem 1 (Law of Large Numbers).

Let $(X_n)_{n \in \mathbb{N}}$ be an infinite sequence of i.i.d. variables with finite expected value. Then:

$$\frac{1}{n} \sum_{i=1}^n X_i \xrightarrow{\text{a.s.}} \mathbb{E}(X_1).$$